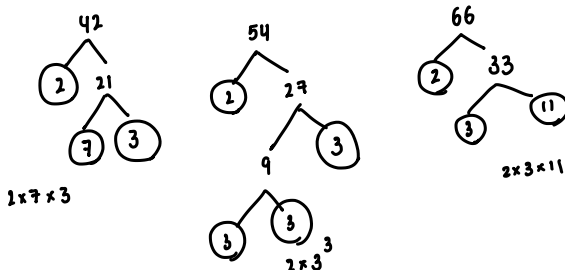




**HCF, LCM**

1. Find, showing your working clearly,  
 (i) the lowest common multiple (*LCM*) of 42, 54 and 66  
 (ii) the highest common factor (*HCF*) of 42, 54 and 66



$$\begin{aligned} \text{i) LCM} &= 2 \times 7 \times 3^3 \times 11 \\ &= 4158 \end{aligned}$$

$$\begin{aligned} \text{ii) HCF} &= 2 \times 3 \\ &= 6 \end{aligned}$$

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- (i) LCM =  
 (ii) HCF =

2.

$$A = 2^3 \times 3 \times 5^2$$
$$B = 2^2 \times 3^2 \times 5 \times 7$$

(i) Find the Lowest Common Multiple (*LCM*) of *A* and *B*.

$$\text{LCM} = 2^3 \times 3^2 \times 5^2 \times 7$$
$$= 12600$$

(ii) Find the Highest Common Factor (*HCF*) of *A* and *B*.

$$\text{HCF} = 2^2 \times 3 \times 5$$
$$= 60$$

3.  $A = 2^3 \times 3^2 \times 5 \times 7$

$B = 2 \times 3^4 \times 5^2 \times 11$

(a) Find the highest common factor (*HCF*) of  $A$  and  $B$ .

(b) Find the lowest common multiple (*LCM*) of  $A$  and  $B$

(c) Find the least number that  $A$  must be multiplied by to give a square number.

$C = 3 \times 10^{205} \times 5 \times 10^{205}$

(d) Work out the value of  $C$ , giving your answer as a number in standard form.

a)  $HCF = 2 \times 3^2 \times 5$   
 $= 90$

b)  $LCM = 2^3 \times 3^4 \times 5^2 \times 7 \times 11$   
 $= 1247400$

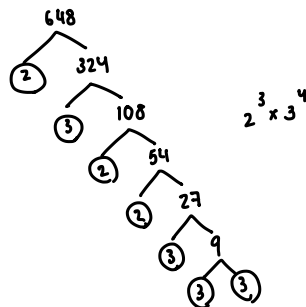
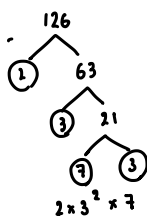
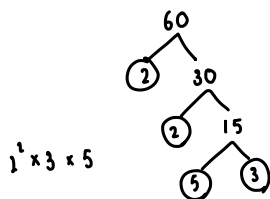
c)  $C = 3 \times 10^{205} \times 5 \times 10^{205}$   
 $= 15 \times 10^{410}$

d)  $15 \times 10^{410} = 1.5 \times 10^{411}$

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4. Find the highest common factor (HCF) of 60, 126 and 648

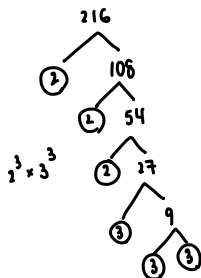
Show your working clearly.



$$\begin{aligned} \text{HCF} &= 2 \times 3 \\ &= 6 \end{aligned}$$

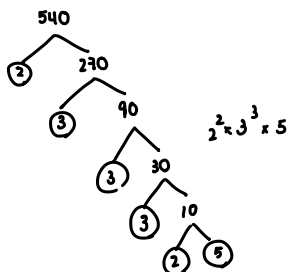
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5. Find the Highest Common Factor (*HCF*) of 216 and 540  
You must show all your working.



$$\text{HCF} = 2^1 \times 3^3$$

$$= 108$$



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6.

$$A = 2^3 \times 3^2 \times 5^4$$

$$B = 2^2 \times 3^3 \times 5^n$$

Given that the Lowest Common Multiple (*LCM*) of *A* and *B* is 3 375 000  
find the value of the integer *n*.

Show your working clearly.

$$LCM = 3\,375\,000$$

$$3\,375\,000 = 2^3 \times 3^3 \times 5^n$$

$$5^n = \frac{3\,375\,000}{216}$$

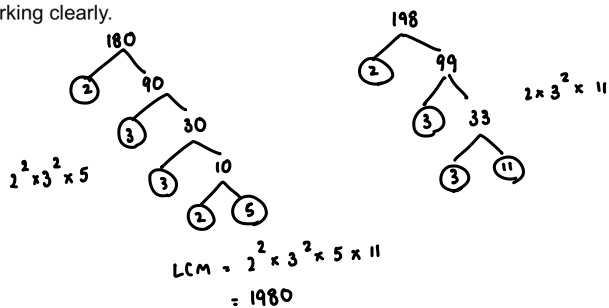
$$5^n = 15\,625$$

$$n = \log_5 15\,625$$

$$n = \underline{\underline{6}}$$

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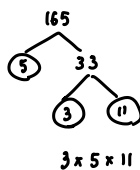
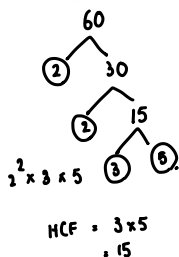
7. Find the Lowest Common Multiple (*LCM*) of 180 and 198  
Show your working clearly.



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8. Find the Highest Common Factor (*HCF*) of 60 and 165  
Show your working clearly.



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9.

$$A = 2^3 \times 3^4 \times 5^3 \times 11$$

$$B = 2^2 \times 3^3 \times 5^4$$

Find the lowest common multiple (LCM) of 2A and 7B

Give your answer as a product of prime factors.

$$2A = 2 (2^3 \times 3^4 \times 5^3 \times 11)$$

$$= 1782\ 000$$

$$7B = 7 (2^2 \times 3^3 \times 5^4)$$

$$= 47\ 2500$$

$$1782\ 000$$

$$891\ 000$$

$$445\ 500$$

$$222\ 750$$

$$111\ 375$$

$$222\ 75$$

$$44\ 55$$

$$891$$

$$297$$

$$99$$

$$33$$

$$11$$

$$2^4 \times 3^4 \times 5^3 \times 11$$

$$LCM = 2^4 \times 3^4 \times 5^4 \times 7 \times 11$$

$$47\ 2500$$

$$67\ 500$$

$$13\ 500$$

$$2700$$

$$540$$

$$108$$

$$2^2 \times 3^3 \times 5^4 \times 7$$

$$54$$

$$27$$

$$9$$

$$3$$